

Nepal Algebra Project(NAP)
Central Department of Mathematics
Tribhuvan University, Kirtipur, Kathmandu, Nepal
Fields and Galois Theory-Preliminary Homework
Course Instructor: Prof. Roger Wiegand and Prof. Sylvia Wiegand

Questions

1. Let R be a commutative ring with $1 \neq 0$. Prove the following statements are equivalent.

(a) $xy = xz, (x \neq 0) \implies y = z$

(b) $x \neq 0, y \neq 0 \implies xy \neq 0$

$$\forall x, y, z \in R$$

2. If p is a prime integer, show that $p \mid \binom{n}{k}$ for $0 < k < p^n$

3. In an integral domain R , show that $a \sim b \iff \langle a \rangle = \langle b \rangle$